



# Indirect Causes in Dynamic Bayesian Networks Revisited

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# Introduction

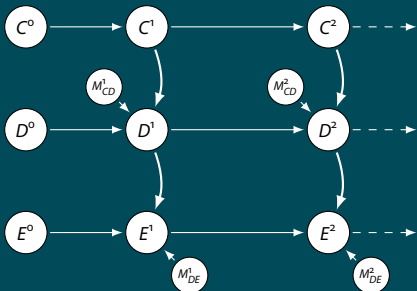
- ▶ Dynamic **Bayesian Networks**.
- ▶ **Indirect** Causes.
- ▶ DAG constraints **limit causal expressiveness**.
- ▶ Solution in DBN semantics on **cyclic graph**.



## Running example

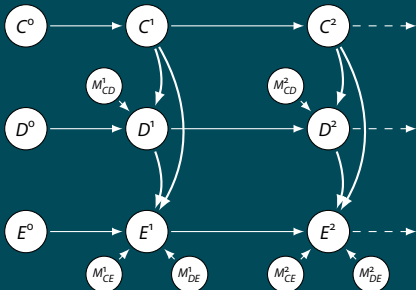
- ▶ **Regulatory compliance** of employees.
- ▶ A “credulous” employee might **manipulate documents**.
- ▶ A credulous employee might (undeliberately) **influence other employees**.
- ▶ Might become credulous too, etc.
  
- ▶ Influences occur through **exchanged messages**.
  
- ▶ Track probabilistic credulousness-state over *time*.
  
- ▶ Employees: **Claire**, **Don** and **Earl**.

## Problem as a DBN



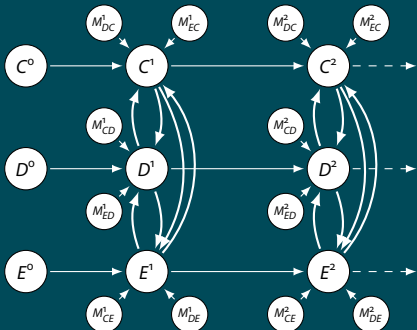
- ▶ Say, only Claire influences Don, influences Earl.
- ▶ i.e. **C influences E indirectly.**
- ▶ Typical DBN. ✓
- ▶ Problem correctly represented. ✓

## Problem as a DBN



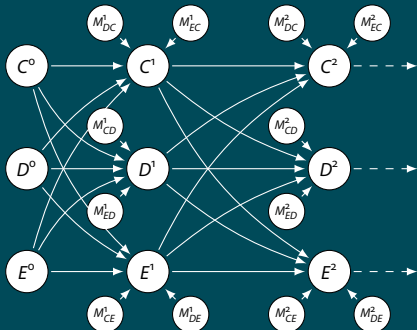
- ▶ Let's add some **more influences**.
- ▶ Claire *can* also influence Earl *directly*.
- ▶ Typical DBN. ✓
- ▶ Problem correctly represented. ✓

## Problem as a DBN



- ▶ Say, **everybody** can influence **everybody**.
- ▶ "A BN is a **DAG**".
- ▶ Not a DBN. **X**
- ▶ Problem correctly represented. **✓?**

## Problem as a DBN



- ▶ Resolve cycles over time.
- ▶ "Diagonal" inter-state dependencies.
- ▶ Common DBN . ✓
- ▶ Problem correctly represented. ~~X~~ ?

## DBN Restrictions

- ▶ “Diagonal” encodes “**incubation time**”:  
*t: Receive Message.  $t + 1$ : Read and become influenced.*

a) Enforces **infinitesimal resolution of time** (e.g., seconds)

✗ High computation cost.

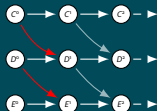


Observations not available this fine (e.g., only daily)?

Computation too costly? Transition only known hourly?

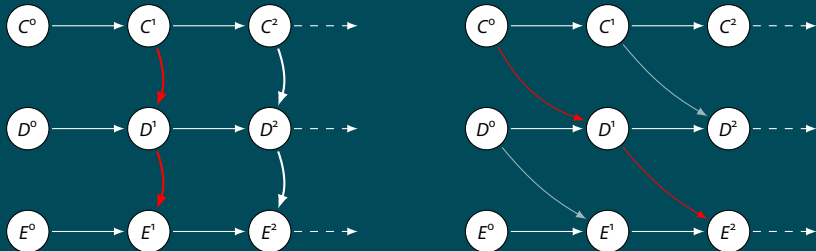
b) **Indirect influences not considerable.**

✗ Does not explain the world.



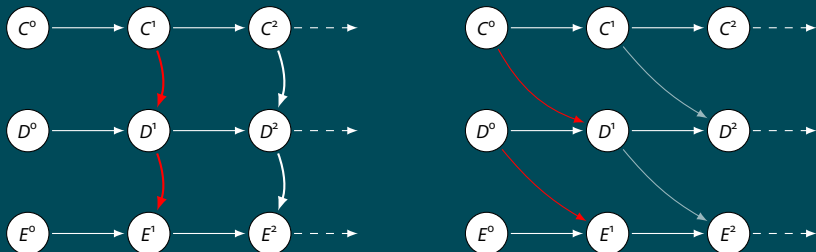


## Classic DBNs spread indirect effects over time



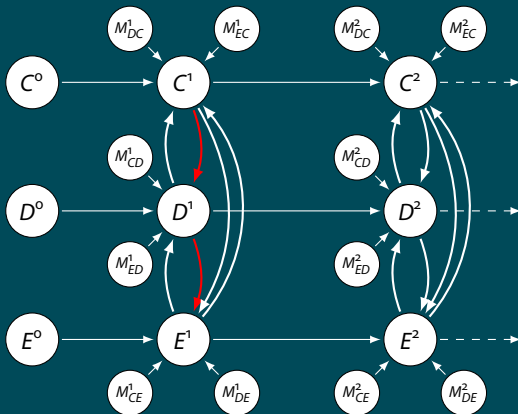
I.e., **observations** that require anticipations of **indirect effects** are **not supported**.

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# Intuitive Design



# Activator Random Variables

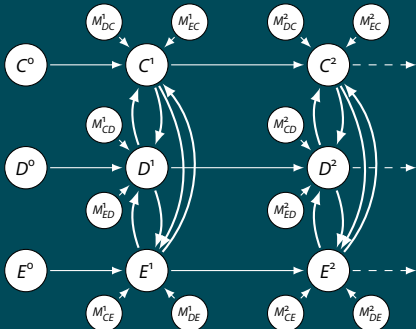
- ▶ Random variables  $M_{XY}^t$  representing exchanged messages are special
- ▶ We see  $M_{XY}^t$  as **Activator Random Variables**

$$\forall x, x' \in \text{dom}(X), \forall y \in \text{dom}(Y), \forall \vec{z} \in \text{dom}(\vec{Z}) : \\ P(y|x, -a_{XY}, \vec{z}) = P(y|x', -a_{XY}, \vec{z}) = P(y|*, -a_{XY}, \vec{z})$$

\* wildcard,  $\vec{z}$  further dependencies

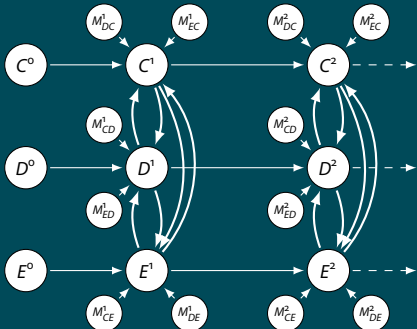
$$\exists x, x^* \in \text{dom}(X), \exists y \in \text{dom}(Y), \exists \vec{z} \in \text{dom}(\vec{Z}) \\ P(y|x, a_{XY}, \vec{z}) \neq P(y|x^*, a_{XY}, \vec{z})$$

# Activator Dynamic Bayesian Networks



- ▶ Is an *Activator Dynamic Bayesian Network*
- ▶ We show: **Semantically a (D)BN**, despite being based on a **cyclic graph!**
- ▶ Straight forward semantic as joint probability as usual.

# Activator Dynamic Bayesian Networks



- ▶ Is an *Activator Dynamic Bayesian Network*
- ▶ We show: **Semantically a (D)BN**, despite being based on a **cyclic graph!**
- ▶ Straight forward semantic as joint probability as usual.
- ▶ Under some restrictions...

# ADBN Restrictions Formally

## Theorem (Bayesian Network Soundness)

For every set of instantiations  $\vec{A}_*^{1:t}$  **an ADBN corresponds to a Bayesian network (BN)**, if for all  $t$ ,  $\vec{A}_*^t$  satisfies a new acyclicity constraint:

$$\forall x, y, z \in \vec{X}^t : \mathfrak{A}(x, z)^t, \mathfrak{A}(z, y)^t \rightarrow \mathfrak{A}(x, y)^t$$

$$\neg \exists q : \mathfrak{A}(q, q)^t,$$

$$\mathfrak{A}(i, j)^t = \begin{cases} \text{false} & \text{if } A_{ij}^t = -a_{ij}^t \\ \text{true} & \text{otherwise} \end{cases}.$$

ADBN's semantics are well-defined as usual in a DBN,

$$P(\vec{X}^{0:t^T}, \vec{A}^{1:t^T}) = P(\vec{X}^{0:t-1^T}, \vec{A}^{1:t-1^T}) \cdot \prod_i P(X_i^t | \vec{X}^{t^T} \setminus X_i^t, \vec{A}_i^{t^T}, X_i^{t-1}) \cdot P(\vec{A}^{t^T}).$$

# Restrictions Comparison

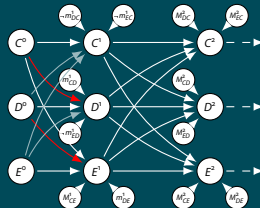
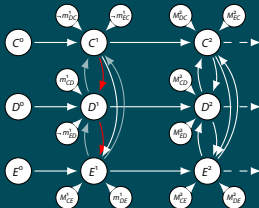
## Cyclic ADBN

- ▶ No cyclic  $M_{XY}^t$  observations allowed.
- ▶ Activator set must form **DAG**.

## “Diagonal” DBN

- ▶ No “interlocking”  $M_{XY}^t$  obs. allowed.
- ▶ must form **bipartite** graph.

#DAG >> #Bipartite







## ADBN Contributions

- ▶ Bayesian networks can syntactically be based on **cyclic** graphs.
- ▶ Cyclic graphs are **causally required** for some problems.
- ▶ Acyclic graphs run into causal problems.

ADBNs provide

- ✓ **Free choice** of time granularity.
- ✓ Anticipation of **indirect influences**.
- ✓ **Well-defined DBN** semantics.
- ✓ **Filtering, Smoothing** same as usual.
- ✓ BN as world-representing first-class declaration.